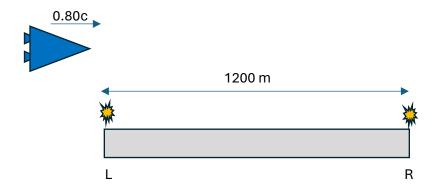
## Teacher notes Topic A

## A specimen paper question on Relativity.

A specimen paper question asks: a rocket moves at 0.80c relative to a space station. Two pulses are emitted from the Left and Right ends of the space station. The pulses are emitted at the same time according to space station observers.



What is the distance between the pulses according to the rocket?

The question is really asking about the distance between the points at which the pulses were emitted.

This is a different question from asking about the length of the space station according to the rocket. To find the length of the space station the rocket must measure the position of the ends of the space station at the same time in the rocket frame. The pulses are not emitted at the same time according to the rocket, so the question is not equivalent to asking about the length of the space station.

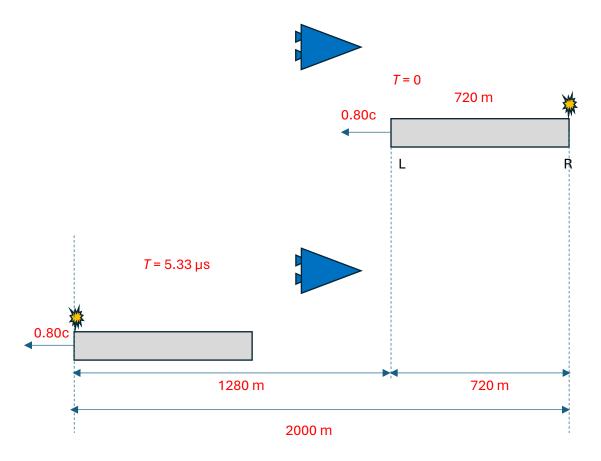
Once we understand this, the answer is simply given by a Lorentz transformation. In the space station frame,  $\Delta x = x_R - x_L = 1200 \text{ m}$  and  $\Delta t = 0$ . Hence,  $\Delta x' = \gamma (\Delta x - v \Delta t) = \frac{5}{3} \times (1200 - 0) = 2000 \text{ m}$ .

We can understand this in this way: the rocket observers think of themselves at rest and the space station is moving to the left with speed 0.80c relative to the rocket. The right pulse is emitted first in the rocket frame. When the right pulse is emitted the left end is a distance equal to the length of the space station away. This length is the Lorentz contracted length of  $\frac{1200}{\frac{5}{2}}$  = 720 m. In the time it

## **IB Physics: K.A. Tsokos**

takes the L pulse to be emitted, the space station moves a distance to the left equal to  $0.80c \times \Delta t'$  where  $\Delta t'$  is the time between emissions according to the rocket. This can be found from another Lorentz transformation:  $\Delta t' = \gamma \left( \Delta t - \frac{v}{c^2} \Delta x \right) = \frac{5}{3} \times \left( 0 - \frac{0.80c}{c^2} \times 1200 \right) = -\frac{16}{3} \times 10^{-6} \text{ s.}$  The minus sign indicates that the right pulse was emitted first. Hence the distance travelled in this time is  $\frac{16}{3} \times 10^{-6} \times 0.80 \times 3 \times 10^8 = 1280 \text{ m.}$  Hence the distance between the points where the pulses were emitted is 720 + 1280 = 2000 m in agreement with the original answer.

The sequence of events is shown below from the point of view of the rocket. The times and distances in red are rocket frame values.



PS

Notice that when the L pulse is emitted the R pulse has travelled a distance of  $\frac{16}{3}\times10^{-6}\times3\times10^{8}=1600~\text{m}.$  So, technically, when the question asked about *the distance between the pulses*, the answer should have been 2000 – 1600=400~m! But I don't think that was the intention.